



The convention used here is:-

- s +ve if direction PO is to the right
- s' +ve if direction $P'O'$ is to the right
- x +ve if direction FO is to the right
- x' +ve if direction $F'O'$ is to the right
- m -ve if image is inverted
- radii +ve if center lies to the right of surface

The focal length f of a thick lens may be calculated using the following formula

$$\frac{1}{f} = (n-1) \left(\frac{1}{r_1} - \frac{1}{r_2} \right) + \frac{(n-1)^2 CT}{nr_1 r_2}$$

The principal plane positions may then be found from

$$VP = \frac{-CT(n-1)f}{nr_2} \quad \text{or} \quad V'P' = \frac{-CT(n-1)f}{nr_1}$$

The magnitude of sag drop on the surface is given by

$$\text{Sag} = \left\{ R^2 - \left(\frac{D^2}{4} \right)^n \right\}$$

where R is the radius of the curvature of that surface and D the diameter of the component.

Many expressions in optics are simplified by considering the power K , given by

$$K = 1/f$$

A common unit of lens power is the diopter which is the power of a lens with a focal length of 1 meter.

In many cases, the center thickness CT produces a second order change to the overall focal length. For a change in wavelength, the focal length f'_λ at a new wavelength λ' can be calculated from the initial focal length f_λ at wavelength λ by the following equation

$$f'_\lambda = f_\lambda \left(\frac{n_\lambda - 1}{n_{\lambda'} - 1} \right)$$

Example 1

To determine the magnification and image position of a BK7 Plano-Convex Lens for an object located 200mm from the curved face

The first principal point P for this lens is located at the curved surface as $VP = 0$.

Taking into account the sign convention $s = -200$ mm. The nominal focal length $f = 40$ mm.

Using the equations on Theory Pg 1 and the information given

$$\begin{aligned} s' &= fs/(f+s) \\ &= 40 \cdot (-200)/(40+(-200)) \\ &= 50\text{mm (measured from } P') \end{aligned}$$

Given $V'P' = -1.6$ mm the paraxial image is formed 48.4 mm from the plano face of the lens.

$$\begin{aligned} \text{Magnification } m &= s'/s \\ &= 50/(-200) \\ &= -0.25 \text{ (the image is inverted)} \end{aligned}$$

Example 2

Solving the same problem using the Newton conjugate equations

$$\begin{aligned} x &= s+f = -200+40 = -160 \text{ mm} \\ x' &= -f^2/x = -(40)^2/(-160) = 10 \text{ mm} \\ m &= f/x = 40/(-160) = -0.25 \\ s' &= x'+f = 10+40 = 50 \text{ mm} \end{aligned}$$